## Supplementary Materials for

# Scaling of Traffic Emissions by Converging Direct Measurements and Mobility Science 

Ayşe Tuğba Öztürk ${ }^{1}$, Helen Fitzmaurice ${ }^{2}$, Olga Kavvada ${ }^{3}$, Philippe Calvez ${ }^{3}$, Ronald C. Cohen ${ }^{4}$, Marta C. González ${ }^{1,5,6 *}$

*To whom correspondence should be addressed. E-mail: martag @berkeley.edu.

## This PDF file includes:

Notes S1 to S6

Figs. S1 to S6

Tables S1 to S2

## Notes <br> S1 Predicting Missing Speed Values with K-Nearest Neighbors Algorithm

Uber Movement API (1) provides hourly speed profiles of street segments in several metropolitan areas starting from 2018. In this project, the time frame between 03/2018 and 12/2019 is analyzed. The data is provided monthly with average speed values and standard deviations of edges. However, speed profiles are not complete and only include road segments that attracted enough traffic in each hour to protect customer privacy. Figure S1 illustrates the boundary of the road network analyzed and data availability for each segment. For each road segment, we averaged the speed values hourly for weekdays and weekends. Meaning for each road we can estimate speed values for at most 48 different time blocks. The blue and light blue road segments in Figure $\mathbf{S} 1$ are where we know the majority of the speed values. While in gray roads we have no data on speeds for any of the time blocks.

Route assignment requires us to know all speed values for all time blocks therefore we utilized machine learning methods to predict the missing speed values. For each road segment, we created spatial, temporal and road type features such as highway type and speed limits. The features we generated for prediction are shown in Table $\mathbf{S 1}$. Then the missing speed values are predicted using the K-nearest neighbors (KNN) algorithm with a k value of 4. The final model had 7 kph mean error in the test set.

## S2 Estimating Travel Demand After Shelter in Place Orders with SafeGraph Data

SafeGraph provides aggregated travel demand data between census block groups for before and after shelter in place (SIP) orders. We use SafeGraph data to estimate the change in the


Fig. S1: Complete Bay Area driving road network and color coded road segments where Uber Movement provided speed data between 2018 and 2019. Observed speeds values are used to get the hourly averages for weekday and weekend speeds which makes 48 time blocks in total.
travel behavior due to SIP between origin and destinations. Then the calculated change is used to scale the TimeGeo travel demand data to get the after SIP travel demand (2). The main

Table S1: Prediction Model Features

| Feature | Description | Type |
| :--- | :---: | :---: |
| speed_kph | Speed limit of the road segment | float |
| sin_hour | $\sin (2 \pi h r / 24)$ where $h r$ is the local city hour between 0-23 | float |
| cos_hour | longitude of the start node of road segment | float |
| start_x | latitude of the start node of road segment | float |
| start_y | longitude of the end node of road segment | float |
| end_x | latitude of the end node of road segment | float |
| end_y | longitude of the centroid of the road segment | float |
| center_x | latitude of the centroid of the road segment | float |
| center_y | Road type of the road segment | Binary, int |
| highway_motorway | Road type of the road segment | Binary, int |
| highway_motorway_link | Road type of the road segment | Binary, int |
| highway_primary | Road type of the road segment | Binary, int |
| highway_primary_link | Road type of the road segment | Binary, int |
| highway_secondary | Road type of the road segment | Binary, int |
| highway_secondary_link | Road type of the road segment | Binary, int |
| highway_trunk | Road type of the road segment | Binary, int |
| highway_trunk_link | Road type of the road segment | Binary, int |
| highway_tertiary | Road type of the road segment | Binary, int |
| highway_tertiary_link | Road type of the road segment | Binary, int |
| highway_residential | Road type of the road segment | Binary, int |
| highway_living_street | Road type of the road segment | Binary, int |
| highway_unclassified |  |  |

challenge at this step is the difference in granularity of the two datasets. TimeGeo data provides origin and destination coordinates for individual travelers, while SafeGraph data is aggregated at census block group level. To be able to perform scaling the two data sets need to be at the
same granularity. We achieve this by rasterizing the two data sets. The steps followed are listed below:

Step 1: Rasterize the SafeGraph data and label each origin and destination census block group with a raster.

Step 2: Calculate the (\%) change in travel demand between the rasterized origin and destinations, $c_{i, j}$, due to SIP orders.

Step 3: Rasterize the TimeGeo travel demand data and calculate the resulting travel demand between the rasterized origin and destinations.

Step 4: Use the $c_{i, j}$ calculated at step 2 to scale the TimeGeo travel demand and get the after shelter in place travel demand estimate between the rasters.

Step 5: Distribute the origin and destination coordinates within their rasters uniformly.

Due to the aggregation-disaggregation involved, we lost information on the home locations of the individual travelers.

## S3 Vehicle Use Rates

At the census tract scale, we obtain the population and the vehicle usage rate of residents in that area. The American Community Survey provides commuting data on the level of census tracts (each containing roughly 5000 people) (3). Supplementary Figure $\mathbf{S 2}$ exhibits the administrative boundaries and share of different commute modes within the regions.

To get an estimate of the vehicle usage rates, we use the following relationship:

$$
\begin{equation*}
\operatorname{VUR}(i)=P_{\text {drive alone }}(i)+\sum_{s=2}^{4} P_{\text {carpool }}^{s}(i) / s, \tag{1}
\end{equation*}
$$

where $P_{\text {drive alone }}(i)$ and $P_{\text {carpool }}^{s}(i)$ are probabilities that residents in zone i drive alone or share a car with $s$ people, respectively.


Fig. S2: Commute modes for the Bay Area census tracts derived from 2019 American Community Survey 1-year estimates

## S4 Calibration of the StreetSmart Parameters

The StreetSmart model does not provide the energy indices for all fuel economies. In order to predict the fuel consumption of a range of vehicle fuel economies, the first step is to estimate the energy indices specific to each vehicle type.

We calibrated the model and obtained the energy index values using the fuel economies reported by the Environmental Protection Agency's (EPA) 2019 Fuel Economy report (4). The EPA uses the FTP-75, a standard speed profile to test for a car's urban fuel economy, and the HTP-75 to test the highway fuel economy (5). We calibrated the model separately for the urban and highway road types. This study used the idle time, travel time, acceleration and distance variables from the FTP-75 and HTP-75 speed profile with the reported fuel economy to calibrate the energy index ranges for each bin shown in Table $\mathbf{S} 2$.

We performed validation against Autonomie softwares vehicle fuel consumption simulations (6) for five different vehicle classes available in the software: Conventional Pickup, Conventional Midsize SUV, Conventional Small SUV, Conventional Compact, Conventional midsize. The resulting mean absolute error percentage is $4.98 \%$ and root mean squared error is 0.68


## S5 Route Assignment and Speed Profiles

Predicting the fuel consumption for each trip in the road network requires a speed profile estimation. Since we don't have the exact routes taken by the travelers, we assign each trip a route in the network given the origin and destination coordinates. In this work we assumed that each traveler will take the route with the shortest travel time. Figure S3A illustrates the route assigned to the trip based on the shortest travel time between the origin and destination pairs.

Fig. S3: An illustrative route assignment and speed profiles associated with the route for a trip given origin and destination coordinates

Once we find the path $P$ traversed by the drivers, we extracted the idle time ( $T_{\text {idle }}$ ), travel time ( $T_{\text {move }}$ ), acceleration (a), and distance $(L)$ variables by checking the properties of the edges

Table S2: Calibrated StreetSmart model parameters considering EPA's 2019 Fuel Economy Report. Fuel efficiency (FE) values are in the units of miler per gallon (mpg). The energy index values, $k_{i}$, are multiplied by $10^{-5}$.

| FE | Road Type | k1 | k2 | k3 | k4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 5 | Highway | 4123 | 117 | 8 | 2068 |
|  | Urban | 94 | 35 | 11 | 2109 |
| 7 | Highway | 3070 | 87 | 6 | 1540 |
|  | Urban | 68 | 27 | 7 | 1523 |
| 9 | Highway | 2526 | 72 | 5 | 1267 |
|  | Urban | 55 | 34 | 3 | 1237 |
| 11 | Highway | 2076 | 59 | 4 | 1041 |
|  | Urban | 46 | 17 | 5 | 1033 |
| 13 | Highway | 1772 | 50 | 3 | 889 |
|  | Urban | 40 | 15 | 5 | 894 |
| 15 | Highway | 1541 | 44 | 3 | 773 |
|  | Urban | 35 | 13 | 4 | 776 |
| 17 | Highway | 1379 | 39 | 3 | 691 |
|  | Urban | 31 | 11 | 3 | 690 |
| 19 | Highway | 1241 | 35 | 2 | 623 |
|  | Urban | 28 | 10 | 3 | 620 |
| 21 | Highway | 1126 | 32 | 2 | 565 |
|  | Urban | 25 | 9 | 3 | 567 |
| 23 | Highway | 1026 | 29 | 2 | 514 |
|  | Urban | 23 | 9 | 3 | 520 |
| 25 | Highway | 952 | 27 | 2 | 478 |
|  | Urban | 21 | 8 | 2 | 479 |
| 27 | Highway | 883 | 25 | 2 | 443 |
|  | Urban | 20 | 7 | 2 | 442 |
| 29 | Highway | 824 | 23 | 2 | 413 |
|  | Urban | 19 | 7 | 2 | 418 |
|  |  |  |  |  |  |


| FE | Road Type | k1 | k2 | k3 | k4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 31 | Highway | 773 | 22 | 1 | 388 |
|  | Urban | 18 | 6 | 2 | 393 |
| 33 | Highway | 728 | 21 | 1 | 365 |
|  | Urban | 16 | 6 | 2 | 368 |
| 35 | Highway | 691 | 20 | 1 | 346 |
|  | Urban | 15 | 6 | 2 | 344 |
| 37 | Highway | 651 | 18 | 1 | 327 |
|  | Urban | 15 | 5 | 2 | 326 |
| 39 | Highway | 619 | 18 | 1 | 311 |
|  | Urban | 14 | 5 | 2 | 309 |
| 41 | Highway | 591 | 17 | 1 | 296 |
|  | Urban | 13 | 5 | 1 | 295 |
| 43 | Highway | 564 | 16 | 1 | 283 |
|  | Urban | 13 | 5 | 1 | 282 |
| 45 | Highway | 539 | 15 | 1 | 270 |
|  | Urban | 12 | 4 | 1 | 270 |
| 47 | Highway | 517 | 15 | 1 | 259 |
|  | Urban | 12 | 4 | 1 | 259 |
| 49 | Highway | 496 | 14 | 1 | 249 |
|  | Urban | 11 | 4 | 1 | 251 |
| 51 | Highway | 477 | 14 | 1 | 239 |
|  | Urban | 11 | 4 | 1 | 238 |
| 53 | Highway | 458 | 13 | 1 | 230 |
|  | Urban | 10 | 4 | 1 | 230 |
| 55 | Highway | 443 | 13 | 1 | 222 |
|  | Urban | 10 | 4 | 1 | 223 |
|  |  |  |  |  |  |

$i$ and nodes at the end of edge $i$ along the path $P$. We estimate the $T_{i d l e}$ by checking the existence of the traffic lights or stop signs. The $T_{\text {move }}$ is calculated using the length $L_{i}$ of the edge $i$ and the speed values $v_{i}$ extracted from Uber Movement Speeds API. We included the acceleration if there is a stop (ie. trip start, trip end, traffic lights) or a speed change (i.e changing from an edge with speed value $v_{i}$ to $v_{i+1}$ ). The braking time ( $T_{\text {brake }}$ ) is acquired from UK highway code (7).

$$
\begin{array}{rll}
T_{\mathrm{i}}^{\text {idle }} & =\left\{\begin{array}{lll}
\mathcal{N}(18,5) & \text { if end node of edge i has a traffic light } \\
3 & \text { if end node of edge } \mathrm{i} \text { is stop sign } \\
0 & \text { otherwise } & \forall i \in P \\
T_{i}^{\text {move }} & =\frac{L_{i}}{v_{i,}} & \forall i \in P \\
a_{i} & =\left\{\begin{array}{ll}
\left|\frac{v_{i}-0}{T_{\text {brake }} \mid}\right| & \text { if there is a stop } \\
\left|\frac{v_{i}-v_{i+1}}{\Delta t}\right| & \text { if there is a speed change }
\end{array} \forall i \in P\right.
\end{array}\right.
\end{array}
$$

Figure S3 B and C illustrates the speed profile and acceleration profiles calculated using the Equations 2,3, and 4.

## S6 Estimating the Emissions from Gallons Fuel Burned

The validation process requires converting the fuel gallons burned to $\mathrm{CO}_{2}$ weight ( grams ) and $\mathrm{CO}_{2}$ flux (micromole $/ \mathrm{m}^{2} / \mathrm{s}$ ). The $\mathrm{CO}_{2}$ weight is used in validation with PEMS-EMFAC model estimates and the $C O_{2}$ flux is used validation with $B E A C O_{2} N$ estimate (8). We used the following equations in our conversions:

$$
\begin{align*}
\text { Fuel }^{g} & =\text { Fuel }^{\text {gal }} \cdot 3795 \frac{\mathrm{ml}}{\mathrm{gal}} \cdot 0.75 \frac{\mathrm{~g}}{\mathrm{ml}}  \tag{5}\\
C^{g} & =\text { Fuel }^{g} \cdot 0.86  \tag{6}\\
C O_{2}^{g} & =C^{g} \cdot \frac{44}{12}  \tag{7}\\
C O_{2}^{\text {flux }} & =C O_{2}^{g} \cdot \frac{1 \mathrm{~mole}}{44 g} \cdot 10^{6} \cdot \frac{1}{A} \cdot \frac{1}{\Delta t} . \tag{8}
\end{align*}
$$

In the calculations, the density of fuel is taken as $0.75 \mathrm{~g} / \mathrm{ml}$ and 0.86 g of $C$ is emitted when 1 gal of fuel is burnt. Note that 1 mole of $\mathrm{CO}_{2}$ weights $44 g$ where $12 g$ of it is $C$. The $A$ in Equation 8 indicates the area.


Fig. S4: Comparison of emissions estimates between PEMS-EMFAC model and MODES for I880, I580 and I980. I880 highway emissions before (A) and during (B) the shelter in place decisions. I580 highway emissions before (C) during (D) the shelter in place decisions. I980 highway emissions before (E) during (F) the shelter in place decisions.


Fig. S5: Tomography of scaling plots for the equation $\beta_{l o c}=\frac{\log \left(Y_{2} / Y_{1}\right)}{\log \left(X_{2} / X_{1}\right)}$ as defined by Barthelemy et. al (9). where $Y_{i}$ is the emissions produced by city $i$ and $X_{i}$ is the independent variable for city $i$. $\beta_{\text {eff }}$ is the mean of the $\beta_{l o c}$ values for the city with the lowest variance in $\beta_{l o c}$ (9). $\beta_{\text {pow }}$ is the scaling coefficient calculated with regular least squares fitting. (A) Tomography of scaling plots where independent variable is population and dependent variable is the emissions. local exponent, $\beta_{l o c}$ converges to $\beta_{e f f}=1.12$ as the ratio $r=\frac{X_{2}}{X_{1}}$ increases. (B) Tomography of scaling plots where independent variable is vehicle kilometers traveled and dependent variable is the emissions. local exponent, $\beta_{l o c}$ converges to $\beta_{\text {eff }}=0.98$ as the ratio $r=\frac{X_{2}}{X_{1}}$ increases.


Fig. S6: Relationship between population density of a city and the congestion levels experienced by the city residents. High population density results in higher congestion levels experienced while at low population density the congestion levels are noisy.


Fig. S7: Relationship between $\alpha$ and $V K T$ for 25 mpg vehicle. The best-fit line is given with the equation $\alpha=\gamma V K T$ where $\gamma=190.6 \pm 33.3$.


Fig. S8: Characteristics of the trips whose predicted emissions are inside (0) and outside (1) the confidence interval. (A) Distribution of the VKT. Majority of the trips' emissions predicted outside the confidence interval are shorter distance trips. (B) Distribution of the idle time per VKT. Trips whose emissions are predicted outside the confidence interval have a larger idle time to VKT ratio. (C) Distribution of the acceleration per VKT. Trips whose emissions are predicted outside the confidence interval have a larger acceleration to VKT ratio.


Fig. S9: Power-law relationship between the VKT multiplier, $\gamma$, and input fuel efficiency. The best fit line is $\gamma=\frac{2006.53 \pm 312.32}{F E}$. Then the full equation to predict the emissions is as follows: $Y=\frac{2006.53}{F E} V K T_{i} \exp \left(\beta_{c}{ }^{F} X\right)$

## References

1. Uber movement speeds. https://movement.uber.com/?lang=en-US. Accessed: 2020-03-01.
2. Xu, Y., Çolak, S., Kara, E. C., Moura, S. J. \& González, M. C. Planning for electric vehicle needs by coupling charging profiles with urban mobility. Nature Energy 3, 484-493 (2018).
3. Bureau., U. C. American community survey 1-year estimates. https://data. census. gov/cedsci/table?q=commute\&tid=ACSST1Y2019.S0801\&moe=false (2019).
4. Fuel economy guide 2019. https://www.fueleconomy.gov/feg/pdfs/ guides/feg2019.pdf. Accessed: 2020-03-01.
5. Agency, E. P. Dynamometer drive schedules. \{https:// www.epa.gov/vehicle-and-fuel-emissions-testing/ dynamometer-drive-schedules\}. Accessed: 2020-03-01.
6. Laboratory, A. N. Autonomie software. https://www.autonomie.net. Accessed: 2020-03-01.
7. Uk highhway code. https://www.highwaycodeuk.co.uk/answers/ what-is-the-stopping-and-braking-distance-of-a-car.
8. Fitzmaurice, H. et al. Assessing vehicle fuel efficiency using a dense network of $\mathrm{co}_{2}$ observations. Atmospheric Chemistry and Physics Discussions 2021, 1-15 (2021). URL https://acp.copernicus.org/preprints/acp-2021-808/.
9. Barthelemy, M. Tomography of scaling. Journal of the Royal Society Interface 16, 20190602 (2019).
